

# Task, hardware, and control: challenges in legged-robot design


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# Robot mobility, on the importance of the design



Why robot mobility ?

- Ground locomotion tasks
- Dynamic and unstructured environment
- Physical interactions + compliance

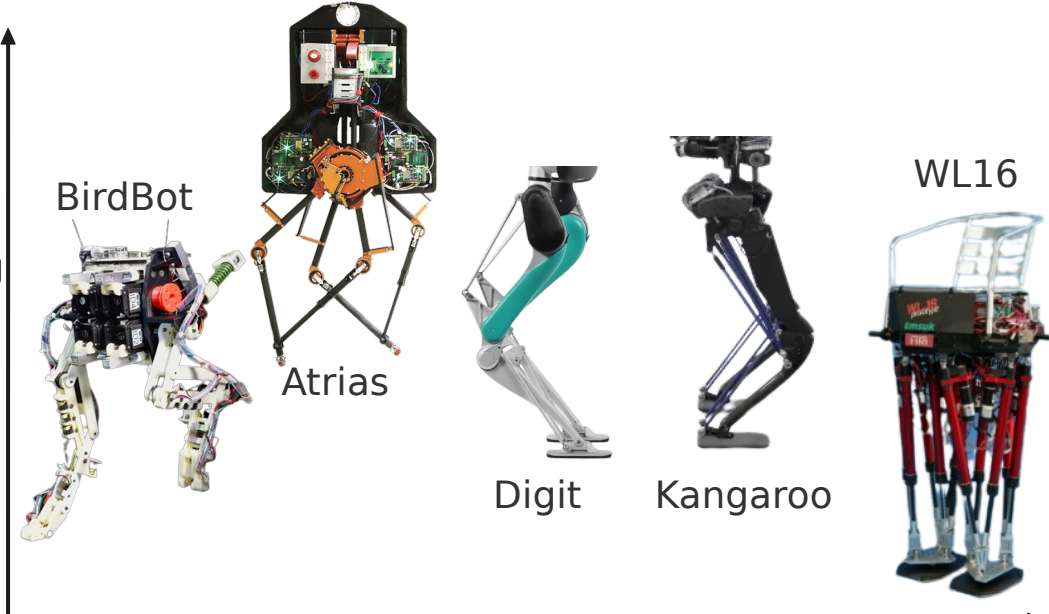
A good design is fundamental for robot mobility

Humanoid robots?

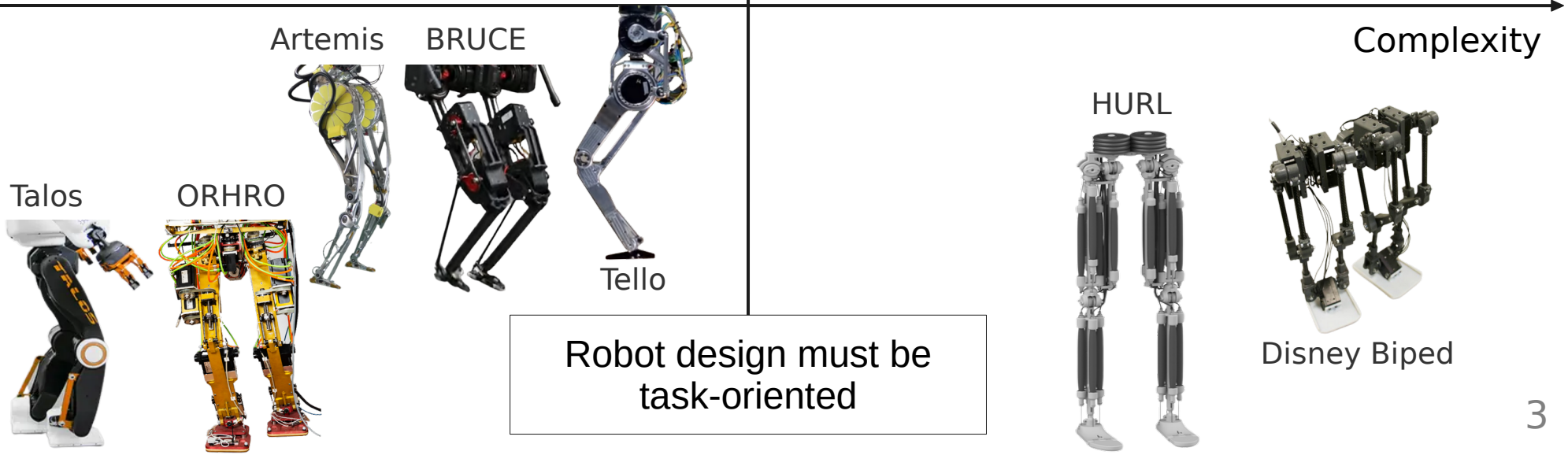
A roboticist ideal but complex

# What is a good design?

Dynamic capability

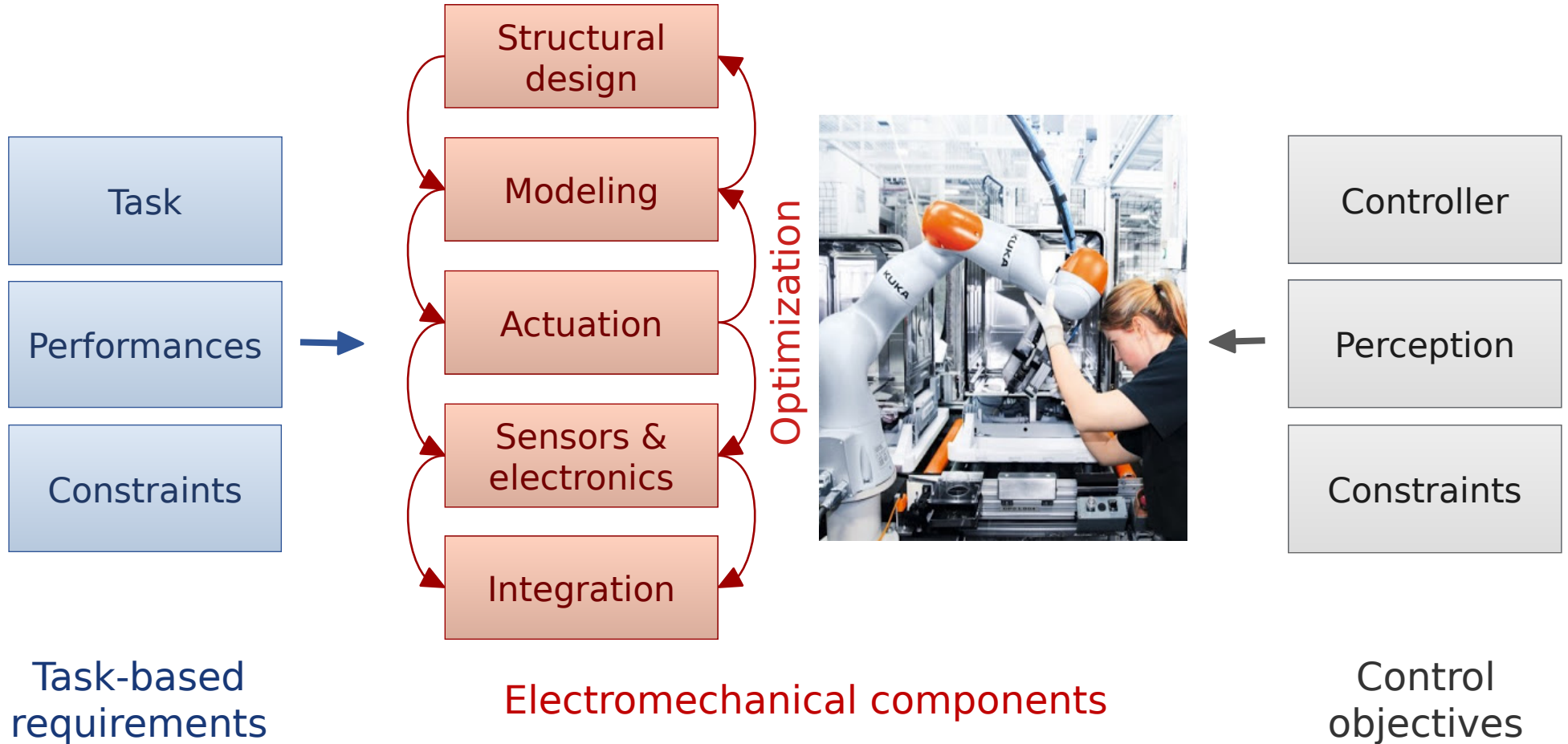


Complexity



Robot design must be task-oriented

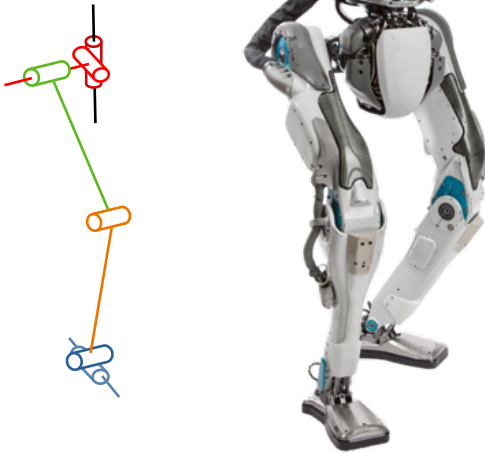
# On the importance of mechatronic design



# Structural design

## Serial legs

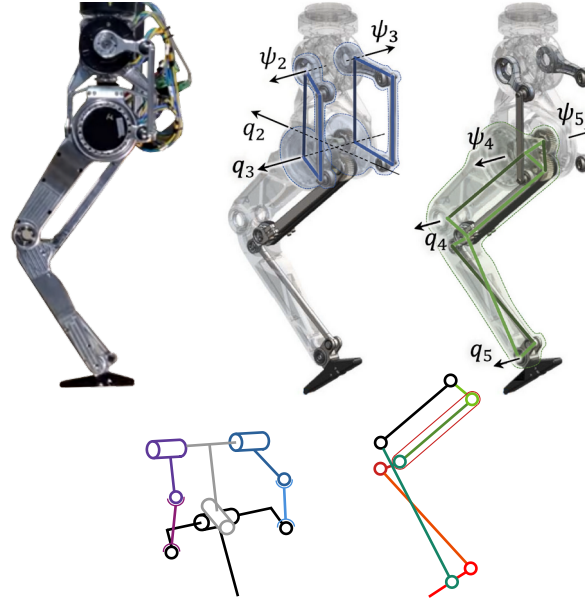
Revolute/prismatic joints



- Large workspace
- High effective inertia
- Reduced force capability
- Structural flexibility
- Small footprint

## Hybrid legs

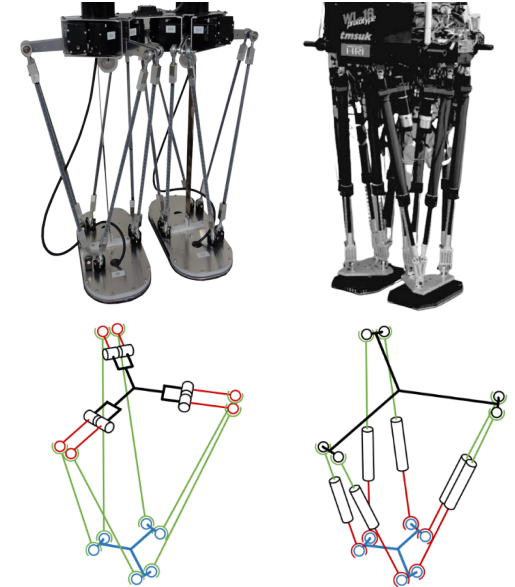
Bar linkage, differential mechanism



- Large workspace
- Low effective inertia
- High force capability
- Improved stiffness
- Small footprint

## Parallel legs

Delta, HEXA, Stewart-Gough



- Limited workspace
- Low effective inertia
- High force capability
- High stiffness
- Large footprint

# Dynamic modeling

- Robot Dynamics libraries

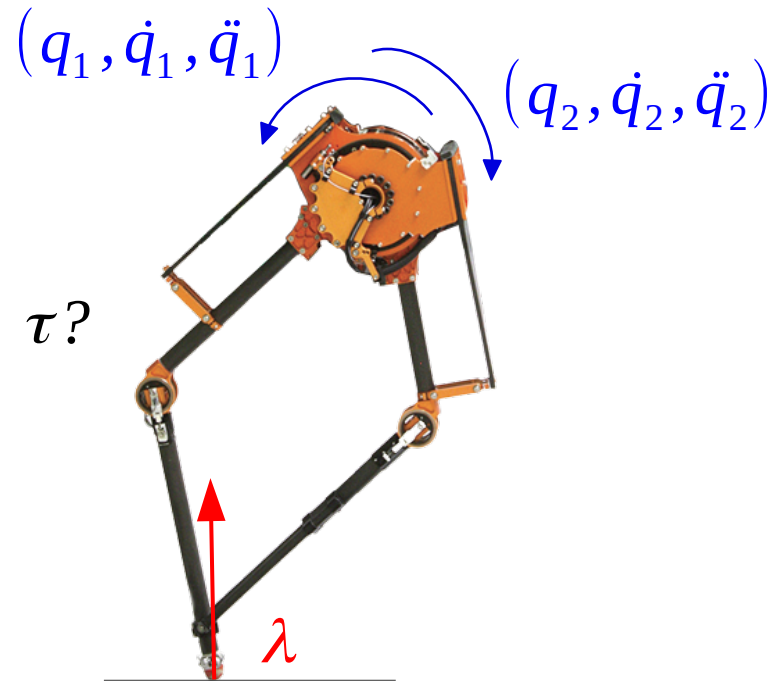
Robot dynamics through Recursive Newton-Euler Algorithm (Pinocchio)

Symbolic model of tree structures (Modélisation Dynamique d'Arborescences)

- Robot description: URDF, SDF

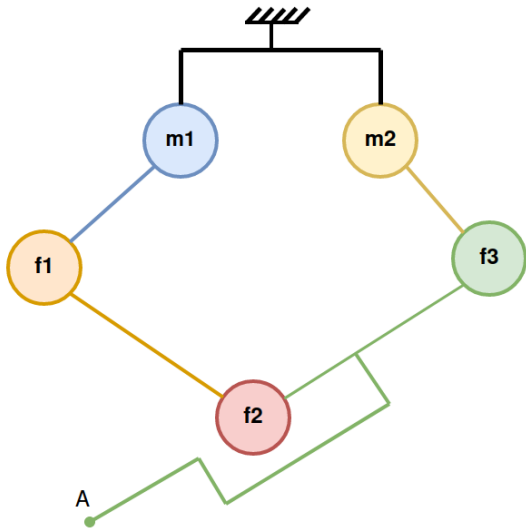
- Closed-loop modeling ?

$$M(q)\ddot{q} + b(q, \dot{q}) + g(q) + G^T \lambda = \tau$$

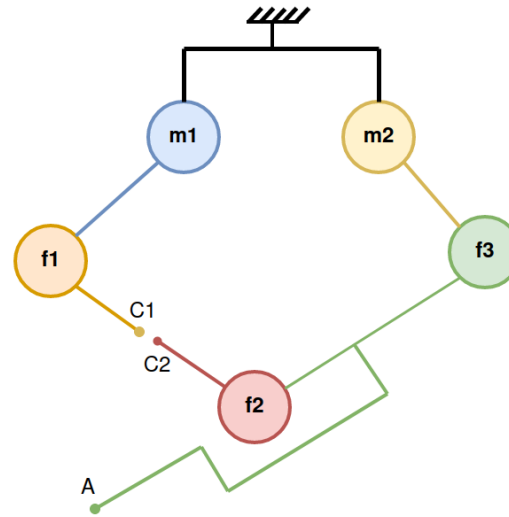


# Closed-loop modeling

## Description of closed loop structure



SDF files  
Any number of  
parent joint by link



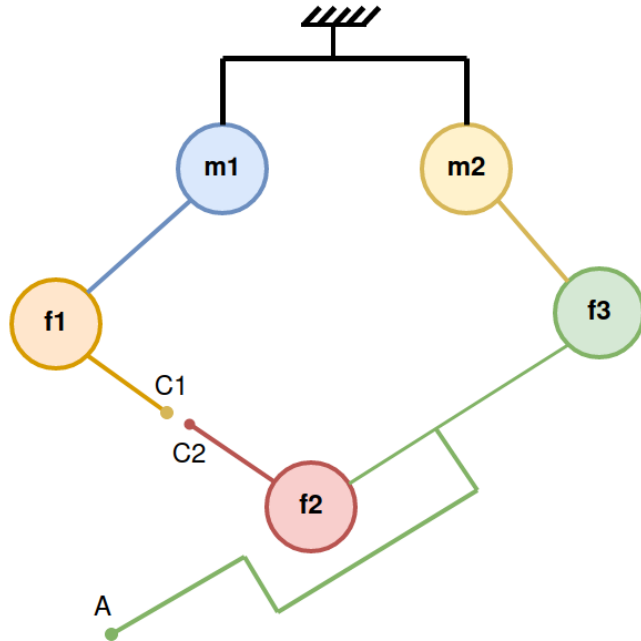
URDF files  
One parent joint by  
link

SDF files led to  
parsing issue =>  
Inertia of the link  
distributed to the joint

URDF files used :  
Robust and reliable  
result for open-loop,  
contact constraint  
generated after

# Closed-loop modeling

## Closed loop jacobian



Contact constraint  
between c1 and c2

With an open loop robot with a contact constraint, define by :

- q its configuration vector
- q\_mot and q\_free the configuration vector of the motor and free joint
- Jc the contact Jacobian ( $Jc = Jc_1 - Jc_2$ )
- Jc = [Jcmot, Jcfree]

We obtain :

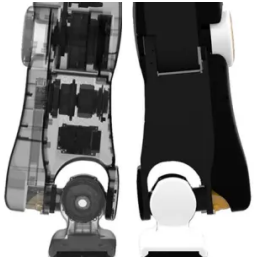
$$\frac{\partial q}{\partial q_{mot}} = \begin{bmatrix} \mathbb{I} \\ -J_{cfree}^\dagger J_{cmot} \end{bmatrix}$$

This led to Jcl, the closed loop jacobian, here in A :

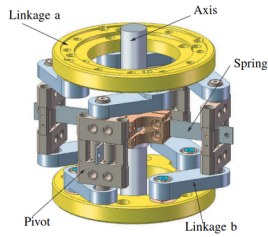
$$J_{cl} = \frac{\partial^o M_A(q)}{\partial q} \frac{\partial q}{\partial q_{mot}}$$



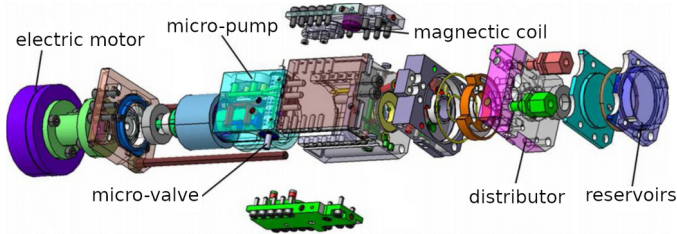
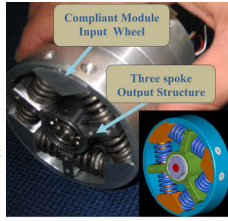
# Actuation



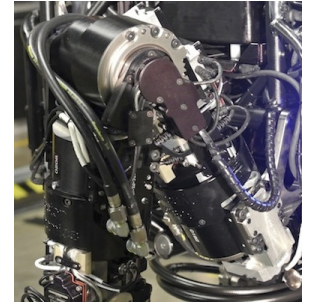
Electric motors  
(DC brushless)



Elastic actuators  
(SEA, VSJ)



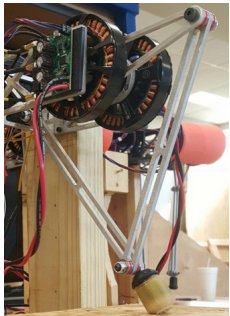
Electro-hydraulic  
actuators (IEHA)



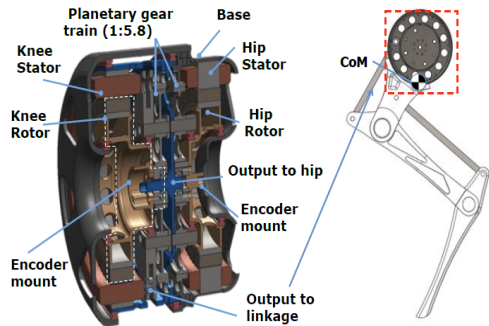
Hydraulic units

High torque, high power to mass ratio, compactness, smooth motion/torque...

**Transmission system** – Mechanical transparency, ratio, flexibility/stiffness



Direct drive  
(Minitaur)



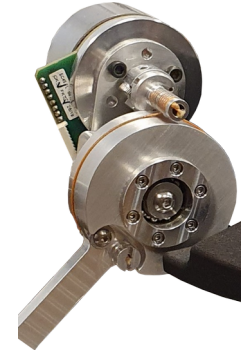
Geared transmission (Cheetah)  
harmonic, planetary, cycloidal



Ball-screw  
(Orhro)

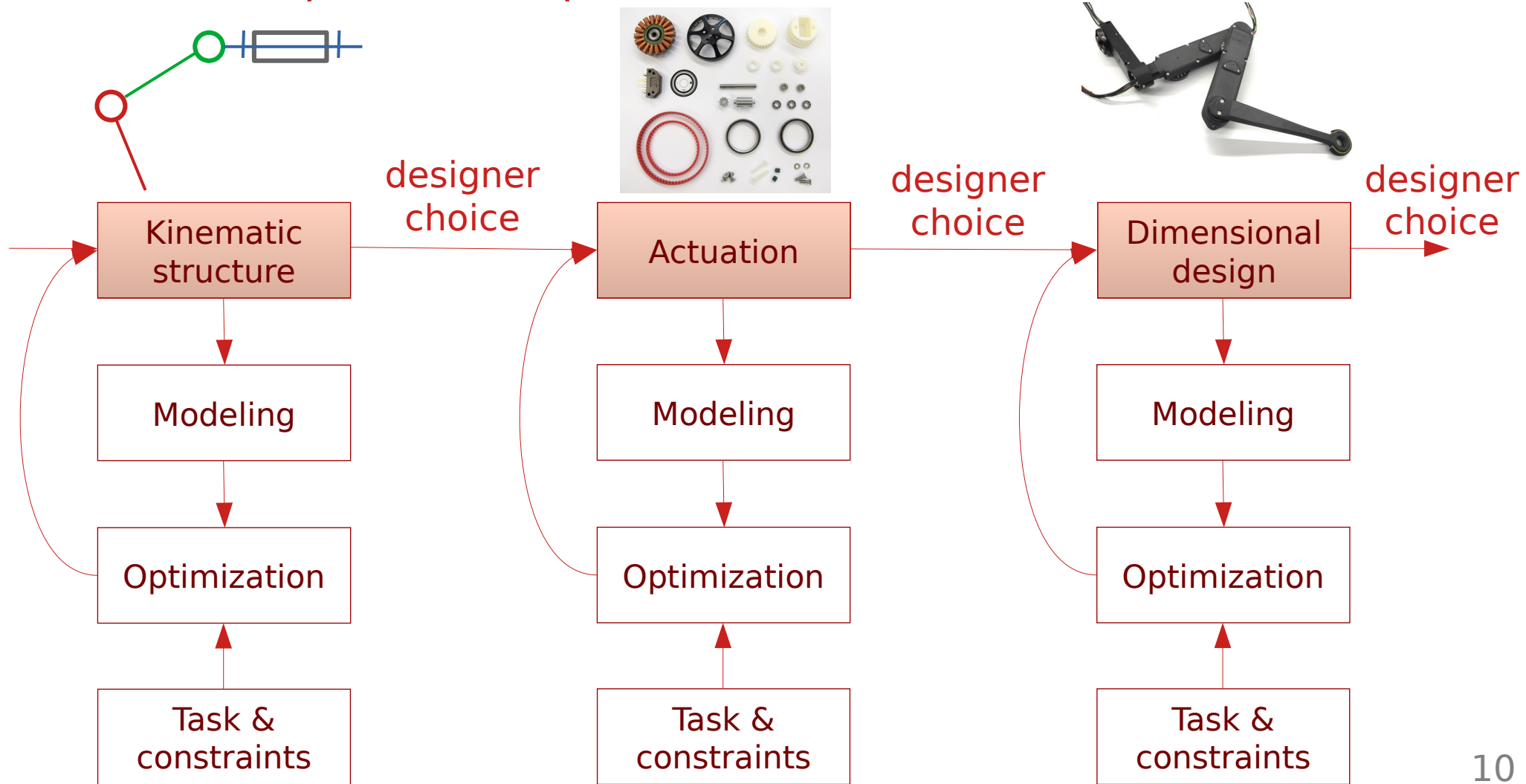


Pulley-Belt  
(Solo)



Cable-driven  
system

# An iterative optimization process



# Common optimization criteria

Workspace

Velocity ellipsoid  $q^T q = v^T (J J^T)^{-1} v = 1$

Kinematic Manipulability  $\omega_c = \sqrt{\det(J J^T)}$

Kinematic Isotropy/Dexterity

$$\eta_c = \frac{\sigma_{\min}(J J^T)}{\sigma_{\max}(J J^T)}$$

Force ellipsoid  $\tau^T \tau = F^T (J J^T) F = 1$

Force Manipulability  $\omega_f = \sqrt{\det(J^{+T} J^+)}$

Force Isotropy/Dexterity

$$\eta_f = \frac{\sigma_{\min}(J^{+T} J^+)}{\sigma_{\max}(J^{+T} J^+)}$$

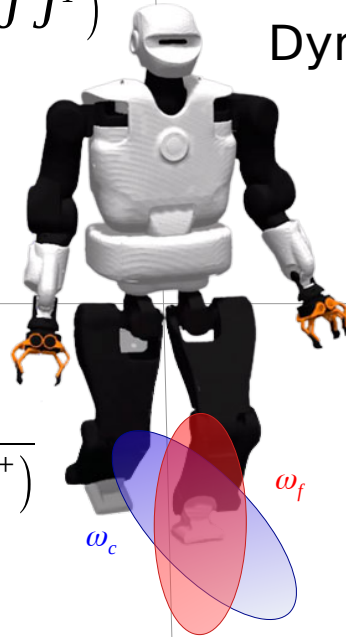
Effective Inertia  $\Lambda = J^{+T} M J^+$

Dynamic ellipsoid  $a^T a = F^T (\Lambda \Lambda^T)^{-1} F = 1$

Dynamic Manipulability  $\omega_d = \sqrt{\det(\Lambda \Lambda^T)}$

Dynamic Isotropy/Dexterity

$$\eta_d = \frac{\sigma_{\min}(\Lambda \Lambda^T)}{\sigma_{\max}(\Lambda \Lambda^T)}$$



Footprint

Joint stiffness  $K_a = k J^{-T} J^{-1}$

Structural stiffness  $K$

Force/motion capability through convex polytopes?

# Leg design criteria

## Formulation

### Kinematics criteria

Rotation Manipulability :

$$RM = \det(Jr_{cl} D r^2 Jr_{cl}^T)$$

Translation Manipulability :

$$TM = \det(Jt_{cl} D t^2 Jt_{cl}^T)$$

Z Reduction Ratio :

$$ZRR = ||Jt_{cl}^T \vec{z}||$$

### Inertial criteria

Foot inertia :

$$\Lambda_{foot} = (J_{closedloop} M_{mot}^{-1} J_{closedloop}^T)^{-1}$$

Foot inertia projected on the z-axis :

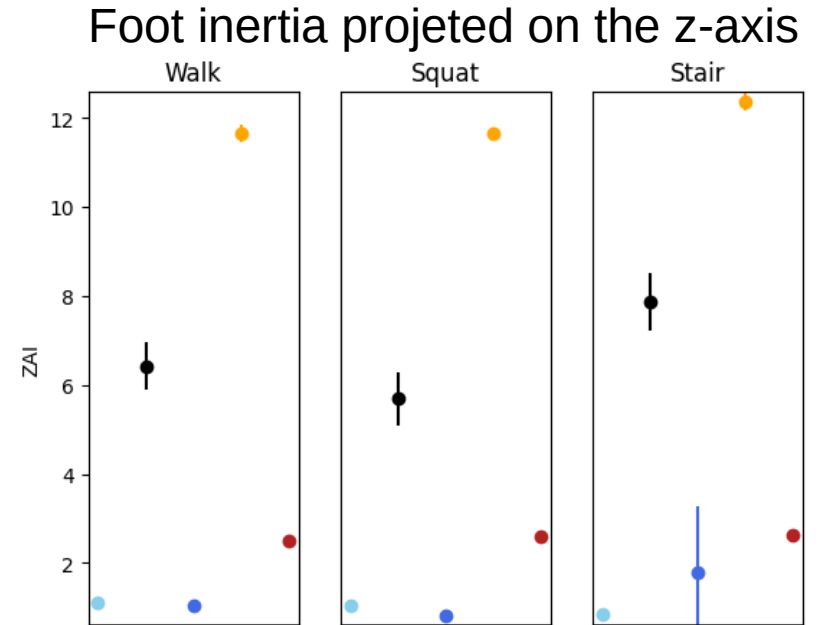
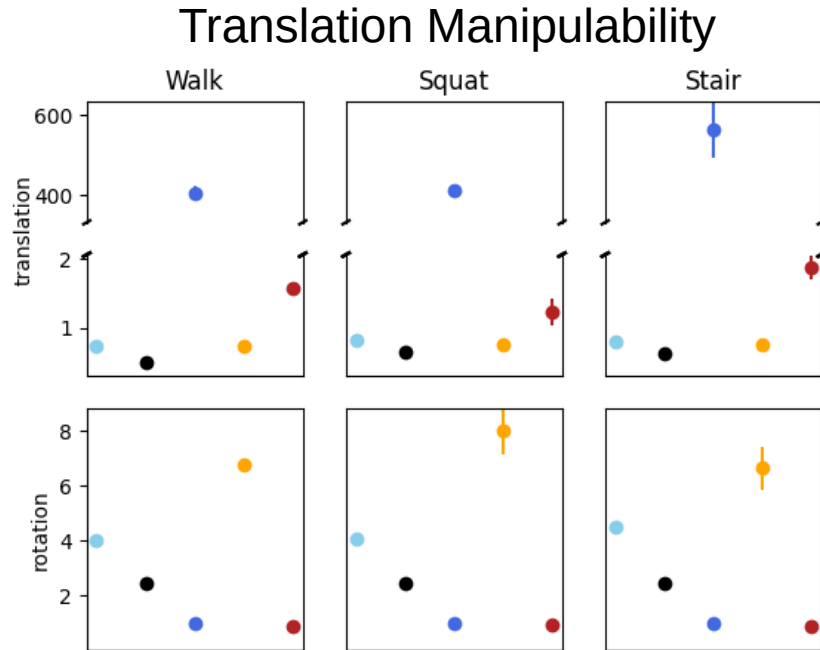
$$ZAI = [z, 0] \Lambda_{foot} [z, 0]^T$$

Impact mitigation factor :

$$IMF = \det(\mathbb{I} - \Lambda_{foot} \Lambda_{Lfoot})$$

# Leg design criteria

## Application



# Optimization problem

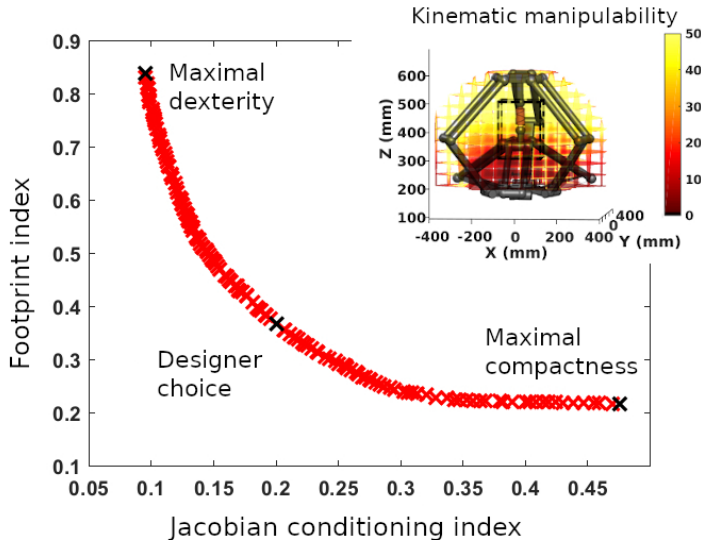
Problem formulation

$$\underset{x}{\text{minimize}} \quad \sum_i \alpha_i f_i(x) \quad \text{subject to} \quad \begin{aligned} g_j(x) &\leq 0 \quad \text{for } j=1\dots m \\ h_k(x) &= 0 \quad \text{for } k=1\dots p \end{aligned}$$

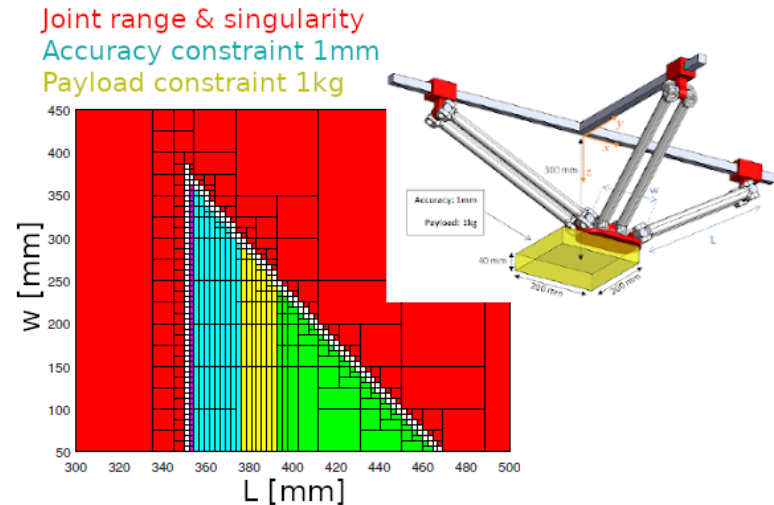
objective functions, weight/penalty, constraints

Aiming at a set of optimal solutions

Pareto front of optimal solutions



Interval-analysis set of feasible solutions

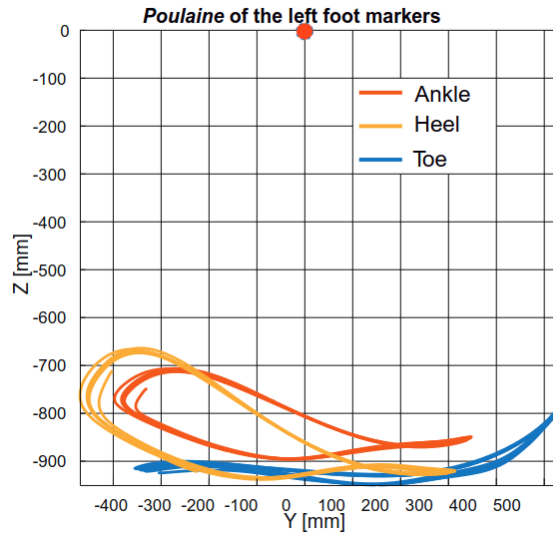


# Locomotion tasks: performances and constraints

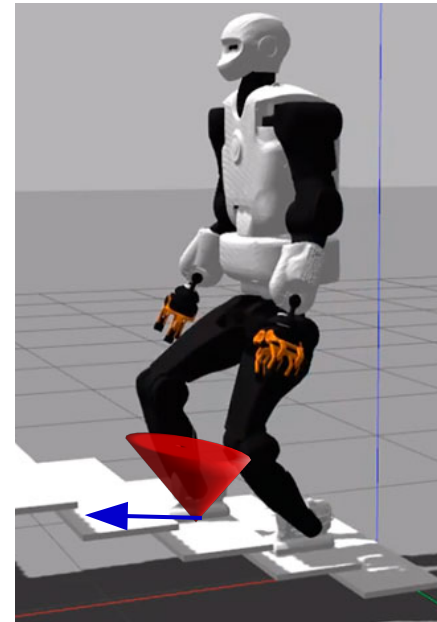
Required performances (task trajectories and force)

Task constraints (workspace, minimal force-motion capability)

Poulaines of walking



Climbing stairs performances



Task variability ?

# Building upon simulation, a codesign approach

