The stack of tasks

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Introduction

Theoretical foundations

Software

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Outline

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The stack of tasks provides a control framework for real-time redundant manipulator control

- implementation of a data-flow,
- control of the graph by python scripting,
- task-based hierarchical control,
- portable: tested on HRP-2, Nao, Romeo.

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Rigid body \mathcal{B}

Configuration represented by an homogeneous matrix

$$M_{\mathcal{B}} = \left(\begin{array}{cc} R_{\mathcal{B}} & \mathbf{t}_{\mathcal{B}} \\ 0 & 0 & 0 & 1 \end{array}\right) \in SE(3)$$

 $R_{\mathcal{B}} \in SO(3) \Leftrightarrow R_{\mathcal{B}}^{\mathsf{T}}R_{\mathcal{B}} = I_3$ and $\det(R) = 1$

Point $\mathbf{x} \in \mathbb{R}^3$ in local frame of \mathcal{B} is moved to $\mathbf{y} \in \mathbb{R}^3$ in global frame:

$$\left(\begin{array}{c} \mathbf{y} \\ 1 \end{array}\right) = M_{\mathcal{B}} \left(\begin{array}{c} \mathbf{x} \\ 1 \end{array}\right)$$

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Rigid body \mathcal{B}

▶ Velocity represented by $(\mathbf{v}_{\mathcal{B}}, \omega_{\mathcal{B}}) \in \mathbb{R}^{6}$ where

 $\dot{R}_{\mathcal{B}} = \hat{\omega}_{\mathcal{B}} R_{\mathcal{B}}$

and

$$\hat{\omega} = \begin{pmatrix} 0 & -\omega_3 & \omega_2 \\ \omega_3 & 0 & -\omega_1 \\ -\omega_2 & \omega_1 & 0 \end{pmatrix}$$

is the matrix corresponding to the cross product operator
Velocity of point P on B

$$\mathbf{v}_{\boldsymbol{p}} = \dot{\mathbf{t}}_{\mathcal{B}} + \omega_{\mathcal{B}} \times \boldsymbol{O}_{\mathcal{B}}^{\mathbf{J}} \boldsymbol{P}$$

where $O_{\mathcal{B}}$ is the origin of the local frame of \mathcal{B} .

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Configuration space

- ► Robot: set of rigid-bodies linked by joints B₀, · · · B_m.
- Configuration: position in space of each body.

$$\mathbf{q} = (\mathbf{q}_{waist}, \theta_1, \cdots, \theta_{n-6}) \in SE(3) \times \mathbb{R}^{n-6}$$
$$\mathbf{q}_{waist} = (x, y, z, roll, pitch, yaw)$$



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• Position of \mathcal{B}_i depends on **q**:

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Velocity:

$$\dot{\mathbf{q}} = (\dot{\mathbf{x}}, \dot{\mathbf{y}}, \dot{\mathbf{z}}, \omega_{\mathbf{x}}, \omega_{\mathbf{y}}, \omega_{\mathbf{z}}, \dot{\theta}_{1}, \cdots \dot{\theta}_{n-6}) \\ \omega \in \mathbb{R}^{3}$$



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- Definition: function of the
 - robot configuration,
 - time and
 - possibly external parameters

that should converge to 0:

$$T \in \boldsymbol{C}^{\infty}(\mathcal{C} imes \mathbb{R}, \mathbb{R}^m)$$

▶ Example: position tracking of an end-effector B_{ee}

- $M(\mathbf{q}) \in SE(3)$ position of the end-effector,
- $M^*(t) \in SE(3)$ reference position

$$T(\mathbf{q},t) = \left(egin{array}{c} \mathbf{t}(M^{*-1}(t)M(\mathbf{q})) \ u_{ heta}(R^{*-1}(t)R(\mathbf{q})) \end{array}
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- t() is the translation part of an homogeneous matrix,
- \overrightarrow{R} and R^* are the rotation part of M and M^*

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Hierarchical task based control

Given

- ► a configuration **q**,
- two tasks of decreasing priorities:
 - ► $T_1 \in C^{\infty}(\mathcal{C} \times \mathbb{R}, \mathbb{R}^{m_1}),$
 - ► $T_2 \in C^{\infty}(\mathcal{C} \times \mathbb{R}, \mathbb{R}^{m_2}),$

compute a control vector q

- ▶ that makes *T*₁ converge toward 0 and
- ▶ that makes *T*₂ converge toward 0 if possible.

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compute a control vector $\dot{\boldsymbol{q}}$

- that makes T_1 converge toward 0 and
- that makes T_2 converge toward 0 if possible.

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Hierarchical task based control

Jacobian:

we denote

•
$$J_i = \frac{\partial T_i}{\partial \mathbf{q}}$$
 for $i \in \{1, 2\}$

► then

 $\blacktriangleright \quad \forall \mathbf{q} \in \mathcal{C}, \forall t \in \mathbb{R}, \forall \dot{\mathbf{q}} \in \mathbb{R}^n, \ \dot{\mathcal{T}}_i = J_i(\mathbf{q}, t) \dot{\mathbf{q}} + \frac{\partial \mathcal{T}_i}{\partial t}(\mathbf{q}, t)$

We try to enforce

$$\dot{T}_1 = -\lambda_1 T_1 \quad \Rightarrow \quad T_1(t) = e^{-\lambda_1 t} T_1(0) \to 0$$

$$\dot{T}_2 = -\lambda_2 T_2 \quad \Rightarrow \quad T_2(t) = e^{-\lambda_2 t} T_2(0) \to 0$$

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Moore Penrose pseudo-inverse

Given a matrix $A \in \mathbb{R}^{m \times n}$, the Moore Penrose pseudo inverse $A^+ \in \mathbb{R}^{n \times m}$ of A is the unique matrix satisfying:

$$AA^{+}A = A$$
$$A^{+}AA^{+} = A^{+}$$
$$(AA^{+})^{T} = AA^{+}$$
$$(A^{+}A)^{T} = A^{+}A$$

Given a linear system:

Ax = b, $A \in \mathbb{R}^{m \times n}$, $x \in \mathbb{R}^n$, $b \in \mathbb{R}^m$

 $x = A^+ b$ minimizes

 $||Ax - b|| \text{ over } \mathbb{R}^n,$

▶ ||x|| over argmin||Ax - b||.

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Hierarchical task based control

Resolution of the first constraint:

$$\dot{T}_1 = J_1 \dot{\mathbf{q}} + \frac{\partial T_1}{\partial t} = -\lambda_1 T_1$$
 (1)

$$J_{1}\dot{\mathbf{q}} = -\lambda_{1}T_{1} - \frac{\partial T_{1}}{\partial t}$$
(2)

$$\dot{\mathbf{q}}_1 \triangleq -J_1^+(\lambda_1 T_1 + \frac{\partial T_1}{\partial t})$$
 (3)

Where J_1^+ is the (Moore Penrose) pseudo-inverse of J_1 . $\dot{\mathbf{q}}_1$ minimizes

- $||J_1\dot{\mathbf{q}} + \lambda_1 T_1 + \frac{\partial T_1}{\partial t}|| = ||\dot{T}_1 + \lambda_1 T_1||$
- $|\dot{\mathbf{q}}|| \text{ over argmin } \|J_1 \dot{\mathbf{q}} + \lambda_1 T_1 + \frac{\partial T_1}{\partial t}\|$

Hence,

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$$J_1 \dot{\mathbf{q}} = -\lambda_1 T_1 - \frac{\partial T_1}{\partial t}$$
(2)

$$\dot{\mathbf{q}}_1 \triangleq -J_1^+(\lambda_1 T_1 + \frac{\partial T_1}{\partial t})$$
 (3)

Where J_1^+ is the (Moore Penrose) pseudo-inverse of J_1 . $\dot{\mathbf{q}}_1$ minimizes

- $||J_1\dot{\mathbf{q}} + \lambda_1 T_1 + \frac{\partial T_1}{\partial t}|| = ||\dot{T}_1 + \lambda_1 T_1||$
- $|\dot{\mathbf{q}}|| \text{ over argmin } \|J_1 \dot{\mathbf{q}} + \lambda_1 T_1 + \frac{\partial T_1}{\partial t}\|$

Hence,

• if
$$\lambda_1 T_1 + \frac{\partial T_1}{\partial t}$$
 is in $Im(J_1)$, (1) is satisfied

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Hierarchical task based control

In fact

$$\forall u \in \mathbb{R}^n, \ J_1\left(\dot{\mathbf{q}}_1 + (I_n - J_1^+ J_1)u\right) = J_1\dot{\mathbf{q}}_1$$

therefore,

$$\dot{\mathbf{q}} = \dot{\mathbf{q}}_1 + (I_n - J_1^+ J_1)u$$

also minimizes $\|J_1\dot{\mathbf{q}} + \lambda_1 T_1 + \frac{\partial T_1}{\partial t}\|$.

 $P_1 = (I_n - J_1^+ J_1)$ is a projector on J_1 kernel: $J_1 P_1 = 0$ $\forall u \in \mathbb{R}^n$, if $\dot{\mathbf{q}} = P_1 u$, then, $\dot{T}_1 = \frac{\partial T_1}{\partial t}$.

The stack of tasks

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$$\dot{\mathbf{q}} = \dot{\mathbf{q}}_1 + P_1 u$$

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We want

$$T_2 = -\lambda_2 T_2$$

Thus

$$-\lambda_2 T_2 = J_2 \dot{\mathbf{q}}_1 + \frac{\partial T_2}{\partial t} + J_2 P_1 u$$
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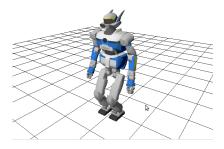
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Example



- T₁: position of the feet + projection of center of mass,
- *T*₂: position of the right wrist.

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The stack of tasks

Outline

Introduction

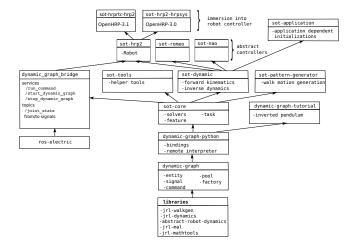
Theoretical foundations

Software

The stack of tasks

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Architecture overview



The stack of tasks

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- jrl-mathtools: implementation of small size matrices,
 - to be replaced by Eigen
- > jrl-mal: abstract layer for matrices,
 - to be replaced by Eigen
- abstract-robot-dynamics: abstraction for humanoid robot description,
- jrl-dynamics: implementation of the above abstract interfaces,
- > jrl-walkgen: ZMP based dynamic walk generation.

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dynamic-graph

Entity

- Signal: synchronous interface
- Command: asynchronous interface
- Factory
 - builds a new entity of requested type,
 - new entity types can be dynamically added (advanced).
- Pool
 - stores all instances of entities,
 - return reference to entity of given name.

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dynamic-graph

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Signal (class SignalTimeDependent)

Synchronous interface storing a given data type

- output signals:
 - recomputed by a callback function, or
 - set to constant value
 - warning: setting to constant value deactivate callback,
- input signals:
 - plugged by an output signal, or
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Synchronous interface storing a given data type

- dependency relation: s1 depends on s2 if s1 callback needs the value of s2,
- each signal s stores time of last recomputation in member s.t_
- s is said outdated at time t if
 - ▶ t > s.t_, and
 - one dependency s_dep of s
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 - has been recomputed later than s: s_dep.t_ > s.t_.
- reading an out-dated signal triggers recomputation.
- New types can be dynamically added (advanced)

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Command

Asynchronous interface

- input in a fixed set of types,
- trigger an action,
- returns a result in the same set of types.

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dynamic-graph-python

Python bindings to dynamic-graph

- module dynamic_graph linked to libdynamic-graph.so
 - class Entity
 - each C++ entity class declared in the factory generates a python class of the same name,
 - signals are instance members,
 - commands are bound to instance methods
 - method help lists commands
 - method displaySignals displays signals
 - class Signal
 - property value to set and get signal value
- remote interpreter to be embedded into a robot controller (advanced)

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dynamic-graph-tutorial

Simple use case for illustration

- Definition of 2 entity types
 - InvertedPendulum
 - input signal: force
 - output signal: state
 - FeedbackController
 - input signal: state
 - output signal: force

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dynamic-graph-tutorial

```
>>> from dynamic_graph.tutorial import InvertedPendulum, FeedbackController
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>>> a = InvertedPendulum ('IP')
>>> b = FeedbackController ('K')
>>> a.displaySignals ()
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Classical inverted pendulum dynamic model
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List of commands:

Integrate dynamics for time step provided as input

take one floating point number as input

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$Class \verb| FeatureAbstract|$

function of the robot and environment states

- position of an end-effector,
- position of a feature in an image (visual servoing)
- ▶ with values in a Lie group $G(SO(3), SE(3), \mathbb{R}^n, ...),$
- with a mapping e from G into \mathbb{R}^m such that

 $e(0_G)=0$

The stack of tasks

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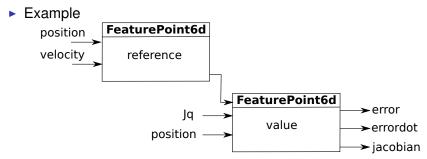
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When paired with a reference, features become tasks.



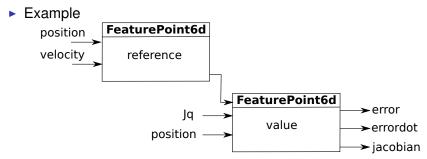
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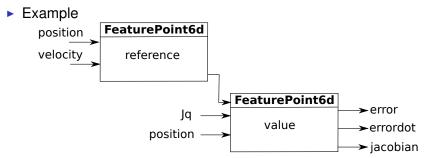


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Feature

When paired with a reference, features become tasks.

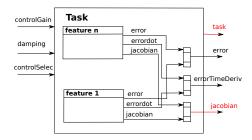


- ▶ error = e(value.position⊖reference.position)
- errordot: derivative of error when value.position
 is constant.

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Task

- Collection of features with a control gain,
- implements abstraction TaskAbstract

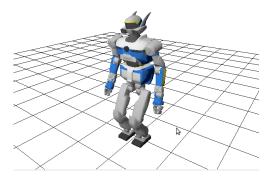


task = -controlGain.error

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Solver SOT

Hierarchical task solver



computes robot joint velocity

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sot-dynamic

dynamic_graph.sot.dynamics.Dynamic builds a kinematic chain from a file and

- computes forward kinematics
 - position and Jacobian of end effectors (wrists, ankles),
 - position of center of mass
- computes dynamics
 - inertia matrix.

sot-pattern-generator

dynamic_graph.sot.pattern_generator

- Entity PatternGenerator produces walk motions as
 - position and velocity of the feet
 - position and velocity of the center of mass

The stack of tasks

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sot-application

dynamic_graph.sot.application

- Provide scripts for standard control graph initialization
 - depends on application: control mode (velocity, acceleration)

The stack of tasks

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Packages specific to robots

sot-hrp2

- defines a class Robot that provides
 - ready to use features for feet, hands, gaze and center of mass,
 - ready to use tasks for the same end effectors,
 - an entity Dynamic,
 - an entity Device (interface with the robot control system)

sot-hrprtc-hrp2

provide an RTC component to integrate sot-hrp2 into the robot controller.

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- dynamic_graph.writeGraph (filename): writes the current graph in a file using graphviz dot format.
- > dynamic_graph.sot.core.FeaturePosition wraps
 two FeaturePoint6d: a value and a reference,
- MetaTask6d:
- MetaTaskPosture:
- MetaTaskKine6d:
- MetaTaskKinePosture:
- MetaTaskCom:

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Utilities

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Installation

Through robotpkg

git clone http://trac.laas.fr/git/robots/robotpkg.git cd robotpkg ./bootstrap/bootstrap --prefix=<your_prefix> cd motion/sot-dynamic

make install

The stack of tasks

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Installation

Through github:

git	clone	recursive	git://github.com/jrl-umi3218/jrl-mal.git
git	clone	recursive	git://github.com/jrl-umi3218/jrl-mathtools.git
git	clone	recursive	git://github.com/laas/abstract-robot-dynamics.git
git	clone	recursive	git://github.com/jrl-umi3218/jrl-dynamics.git
git	clone	recursive	git://github.com/jrl-umi3218/jrl-walkgen.git
git	clone	recursive	git://github.com/jrl-umi3218/dynamic-graph.git
git	clone	recursive	git://github.com/jrl-umi3218/dynamic-graph-python.git
git	clone	recursive	git://github.com/jrl-umi3218/sot-core.git
git	clone	recursive	git://github.com/laas/sot-tools.git
git	clone	recursive	git://github.com/jrl-umi3218/sot-dynamic.git
git	clone	recursive	git://github.com/jrl-umi3218/sot-pattern-generator.git
git	clone	recursive	git://github.com/stack-of-tasks/sot-application.git
git	clone	recursive	git://github.com/laas/sot-hrp2.git
git	clone	recursive	git://github.com/stack-of-tasks/sot-hrprtc-hrp2.git

for each package,

```
mkdir package/build
cd package/build
cmake -DCMAKE_INSTALL_PREFIX=<your_prefix> .
```

make install

The stack of tasks

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Installation

Through github:

git clone --recursive git://github.com/jrl-umi3218/jrl-mal.git git clone --recursive git://github.com/jrl-umi3218/jrl-mathtools.git git clone --recursive git://github.com/jrl-umi3218/jrl-dynamics.git git clone --recursive git://github.com/jrl-umi3218/jrl-dynamics.git git clone --recursive git://github.com/jrl-umi3218/dynamic-graph.git git clone --recursive git://github.com/jrl-umi3218/dynamic-graph.git git clone --recursive git://github.com/jrl-umi3218/dynamic-graph.git git clone --recursive git://github.com/jrl-umi3218/dynamic-graph.git git clone --recursive git://github.com/jrl-umi3218/sot-core.git git clone --recursive git://github.com/jrl-umi3218/sot-dynamic.git git clone --recursive git://github.com/jrl-umi3218/sot-dynamic.git git clone --recursive git://github.com/jrl-umi3218/sot-dynamic.git git clone --recursive git://github.com/jrl-umi3218/sot-pattern-generator.git git clone --recursive git://github.com/jrl-umi3218/sot-pattern-generator.git git clone --recursive git://github.com/stack-of-tasks/sot-hprptc-hrp2.git

for each package,

```
mkdir package/build
cd package/build
cmake -DCMAKE_INSTALL_PREFIX=<your_prefix> ...
```

make install

The stack of tasks

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Installation

Through installation script

git clone git://github.com/stack-of-tasks/install-sot.git cd install-sot/scripts

./install_sot.sh

The stack of tasks

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Running the stack of tasks into OpenHRP-3.1

You need to install:

- ▶ ros-electric
- ▶ OpenHRP-3.1

you will find instructions in https://wiki.laas.fr/robots/HRP/Software Then follow instructions in sot-hrprtc/README.md:

https://github.com/stack-of-tasks/sot-hrprtc-hrp2

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Running the stack of tasks into OpenHRP-3.0.7 Assumptions

- OpenHRP 3.0.7 is installed
- The Stack of Tasks has been installed thanks to previous slide with install_sot.sh in the directory:

/home/user/devel/ros_unstable

> Your /opt/grx3.0/HRP2LAAS/bin/config.sh is well setup.

The golden commands

\$>roscore
#Launching HRP2 simulation with OpenHPR
\$>roslaunch hrp2_bringup openhrp_bridge.launch robot:=hrp2_14
mode:=dg_with_stabilizer simulation:=true
\$>rosservice call /start_dynamic_graph
\$>rosrun dynamic_graph_bridge run_command

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Running the stack of tasks into OpenHRP-3.0.7

Initialize the application: create tracer and solver

```
[INFO] [WallTime: 1370854858.786392] waiting for
service...
Interacting with remote server.
>>> from dynamic_graph.sot.application.velocity.\\
precomputed_tasks import initialize
>>> solver = initialize (robot)
>>> robot.initializeTracer ()
```

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Running the stack of tasks into OpenHRP-3.0.7

Build the graph including the pattern generator

[INFO] [WallTime: 1370854858.786392] waiting for service... Interacting with remote server. >>> from dynamic_graph.sot.pattern_generator.walking import CreateEverythingForPG, walkFewSteps With meta selector

Running the stack of tasks into OpenHRP-3.0.7

Create the graph

```
>>> CreateEverythingForPG(robot, solver)
At this stage
('modelDir:_',
    '~/devel/ros-unstable/install/share/hrp2-14')
('modelName:', 'HRP2JRLmainsmall.wrl')
('specificitiesPath:',
    'HRP2SpecificitiesSmall.xml')
('jointRankPath:', 'HRP2LinkJointRankSmall.xml')
After Task for Right and Left Feet
```

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Running the stack of tasks into OpenHRP-3.0.7

Switch to the new graph

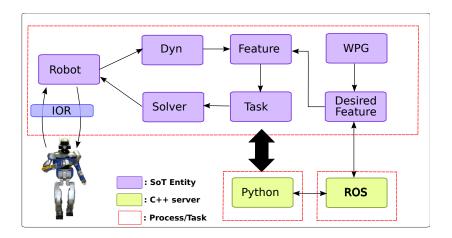
>>> walkFewSteps(robot)

The stack of tasks

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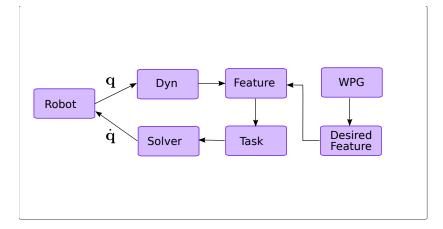
Software structure - Conceptual view



The stack of tasks

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Software structure - Link with Model

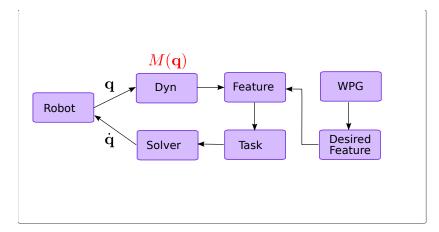


The stack of tasks

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₹ 990

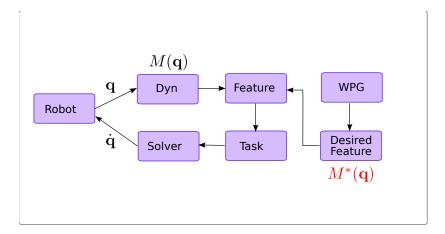
Software structure - Link with Model



The stack of tasks

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Software structure - Link with Model

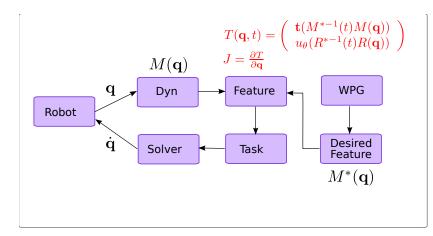


The stack of tasks

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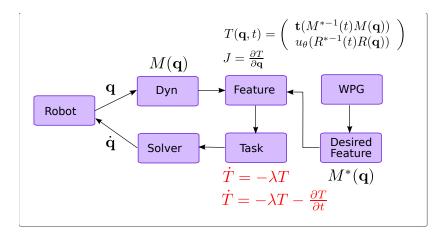
Software structure - Link with Model



The stack of tasks

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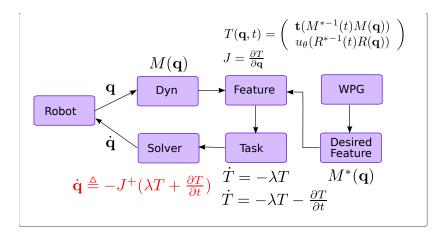
Software structure - Link with Model



The stack of tasks

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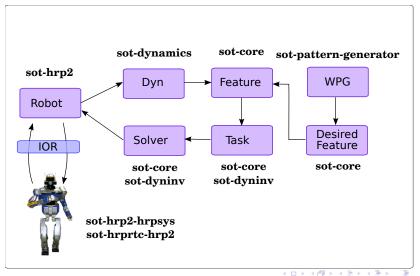
Software structure - Link with Model



The stack of tasks

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Software structure - Repositories



The stack of tasks